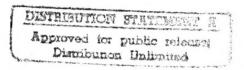


FOA Rapport D--95--00153-1.1,1--SE September 1995



# The Lanchester Theory of Combat and Some Related Subjects.

A Bibliography 1900 - 1993



Staffan Wrigge Arne Fransén Lars Wigg

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FÖRSVARETS FORSKNINGSANSTALT
Avdelningen för Försvarsanalys
172 90 STOCKHOLM Tel 08-706 30 00

4 December, 1995

US Army Concepts Analysis Agency ATTN: CSCA-TA (Dr. Robert L. Helmbold) 8120 Woodmont Avenue Bethesda, Maryland 20814-2797

Defense Technical Information Center (DTIC-OCP) 8725 John J. Kingman Road, Suite 0944 Ft. Belvoir, VA 22060-6218

Re: Transmittal of Report, "The Lanchester Theory of Combat and Some Related Subjects: A Bibliography 1900-1993"

- 1. The enclosed report, "The Lanchester Theory of Combat and Some Related Subjects: A Bibliography 1900-1993," FOA Report D--95--00153-1.1,1--SE, September 1995, is submitted for archiving in the DTIC collection.
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Dr. Robert L. Helmbold

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GS-14, CSCA-TA



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November 6, 1995

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Your reference

Our reference

#### Dear Sir:

Thank you very much for your two letters and your kind words about our Lanchester bibliography. Your lists of references will certainly be helpful — expecially regarding the development during the last 10 years or so — in case we get the time to issue a revised edition of the bibliography. In fact, my colleague Staffan Wrigge was so stimulated by your letter that he already has proposed such an idea and is prepared to take part in the work. It is too early for myself to say if my time will permit this. By the way, Mr. Wrigge who has corresponded with you about the Russian Osipov, sends his greetings to you.

Now for your question about forwarding the report to DTIC and NTIS. Our report administration group already has sent a copy to the NTIS, so I assume they will make it known through their usual channels (GRA etc.) If you, however, think the report will be made known by more readers, or made known by the "Lanchester community" more effectively by sending it to the DTIC, then I certainly endorse your doing so.

In your second letter of 19 October your have furnished us with very valuable information about the addresses of some researchers in the field. I suppose this is the result of a letter I sent to the Military Operations Society of America asking for such help. Your name was included in the list of people, whose addresses we asked about, to be quite sure that we sent the report to the correct address. It is our understanding that many organizational changes have been made within the U.S. Defense lately, so we thought maybe also the CAA had been influenced. By a mistake our report administrators sent a copy to you instead of awaiting the result of our inquiries.

We have tried to send copies to about 30 American authors of articles and books on Lanchester theory. All of them are mentioned in our bibliography. If you, however, know of other researchers who you think should receive our report, please inform me about them. I also enclose a couple of copies for your own use.

Sincerely,

Address:

Lars Wigg

Lus Wy

National Defence Res. Establishment (FOA)

S-172 90 STOCKHOLM, Sweden

Enclosure

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Int +46 8 706 30 00

Telex

# The Lanchester Theory of Combat and Some Related Subjects. A Bibliography 1900-1993

Staffan Wrigge Arne Fransén Lars Wigg

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#### **Preface**

This report is the joint work of three persons, all of whom have worked for many years at the National Defence Research Establishment (FOA) in Sweden. We have all been involved in making models of different aspects of battles including all the military services. During this work we have come into contact with the Lanchester theory of combat which we consider as an important tool in model building.

Two of us, S Wrigge and L Wigg, have systematically gathered information concerning Lanchester theory since the early 1970s. In 1975 we compiled a bibliography on the subject. Since then twenty years have passed and quite a few papers (reports, books) about Lanchester theory have seen the daylight. Thus we have found time to be ripe for a new bibliography, which is presented here.

The third of us, Arne Fransén, has contribued with his expert knowledge of computers and data bases. He has arranged all the information in a data file. He has also carefully checked many of the references against the original documents (or microfiches thereof).

It can hardly be claimed that this bibliography is complete. This is emphasized by the complement at the end of section 7 in Appendix A. This complement is mainly the result of a study of the reference lists of a number of Lanchester reports.

We welcome, of course, all comments on this bibliography as well as corrections and additions. Those should be sent to Lars Wigg, FOA, S-172 90 Stockholm, Sweden. (The other two authors will soon be leaving FOA.)

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# **INTRODUCTION**

# 1. Definitions and general background

The Lanchester theory of combat is most easily defined as a mathematical description of the course and outcome of real or simulated battle or of situations of a similar nature - such as the struggle for market shares. The tools which are used are most often differential equations and/or stochastic processes. The "Lanchesterians" consider their theory of battle as a part of physics (see e.g. Brackney (86)).

The theory has received its name from one of its creators, F W Lanchester (1868-1946), an English gentleman of numerous talents and interests. Its other creator was for many years virtually unknown in the West. His name was M Osipov (18??-19??), and his background is so obscure that it is not even known what the initial "M" stands for. Both Lanchester's and Osipov's work is from the 1914-1916 period. Since they worked independently of one another, one should properly speak of the Lanchester-Osipov theory of combat. We believe that this designation will become customary among military analysts in the future.

A more detailed description of Lanchester's life and work is to be found in the references given in section 2.1. Although far less complete, the corresponding data for Osipov is given in section 2.3. (A predecessor of both is the American officer B A Fiske, who as early as 1905 published a simple discrete version of one of the Lanchester-Osipov equations (see especially section 2.1).)

The title of this bibliography includes the words "and some related subjects". This refers mainly to mathematical models of duels, which is a well-defined area of research. Another area included is movement of the frontline in battles or campaigns. There are also studies of the frequency, duration and extent of labour strikes and of wars. As mentioned above, we have also included references to papers treating struggles for market shares and similar competitive situations. Finally, we have included references to more extensive combat models which we know or strongly believe are built upon Lanchester theory.

In a previous bibliography (Wrigge & Wigg (615)) biological combat models were also mentioned, since there are many connections between these and Lanchester theory: methods of reasoning and the resulting differential equations are similar in both cases. For reasons of space, however, we have not included these references in the present work.

Surveys of Lanchester models (deterministic and/or stochastic) or of models of duels have been made by C J Ancker (13), C J Ancker & A V Gafarian (19), J Byrne & A Lamontagne (100), L Dolanský (151), L K Ekchian (158), B W Fowler (187, 188), G S Hall (229), N K Jaiswal (295), A F Karr (315), and J G Taylor (538-540). Both an annotated and unannotated bibliography has been compiled by J G Taylor (540). Other lists of valuable references have been included in G S Hall (229) and L Dolanský (151), and an unofficial bibliography was published by P J Haysman and B E Mortagy (246). See also the bibliography by S Wrigge & L Wigg (615).

## 2. A historic survey

# 2.1 United States and Western Europe (except Sweden)

In our part of the world the pioneer of the mathematical description of combat is, as has already been mentioned, the Englishman F W Lanchester. His basic and often quoted book "Aircraft in Warfare - The Dawn of the Fourth Arm" appeared in 1916. In order to strengthen his military thesis Lanchester was forced to analyze relations between the combatants in different kinds of combat. He published many of his ideas in 1914 in the journal Engineering. A documentation of Lanchester's life and work is given by T von Karman (308), P W Kingsford (338), J F McCloskey (373) and H R Rickardo (440).

In 1905 B A Fiske published a discrete version of one of Lanchester's equations. In a later work, Fiske (184), there is a reference to J V Chase, who published similar results in 1902. As far as we know, this is the earliest reference to what would later be known as the Lanchester-Osipov theory of combat. Fiske's work is discussed by H K Weiss (592) and J H Engel (163).

In the 1920's and 30's the development of the mathematical theory of combat took place mainly in that branch of mathematical biology which deals with the

balance between predators and preys. Important contributions were made by C F Gause, J Lotka and V Volterra.

After the World War II, intensive studies of this subject were made at several American universities and military research institutes. Masses of data from WWII and earlier wars were gathered and analyzed in order to test and develop the Lanchester theory. Contributions by J H Engel (162, 164) and H K Weiss (594) should be mentioned. Lanchester combat theory has been weak when it comes to verification and validation. This painstaking activity almost ceased for a while but was resumed in the 80's and 90's. In this context, works by T N Dupuy (155, 156) and D S Hartley (237-244) can be mentioned.

The main body of references in this bibliography consists of papers, reports and theses produced in the US. Many originate at military research institutes such as the Naval Postgraduate School in Monterey, California and the Institute for Defense Analyses in Arlington, Virginia. As regards Europe, much valuable work has been done in the United Kingdom at DOAE and, to some extent, at the Royal Military College; in Italy at SACLANT ASW Research Centre; in Netherlands at SHAPE Technical Centre; in Germany at IABG in Munich; in Sweden at FOA; in Austria at Institut für Grundlagenforschung an der Landesverteidigungsakademie; and in Switzerland at various institutes and operations research sections within the military establishment.

Our knowledge of what has been done in Lanchester theory and associated areas is of necessity incomplete i.a. because of military classification. Compared with an earlier version of this bibliography from 1975, however, we have been able to fill in several gaps.

In section 3 more details will be given about individual researchers and research institutes.

2.2 Sweden: The National Defence Research Establishment (FOA)

As early as the 1950's, FOA developed a serious interest in Lanchester theory and other mathematical descriptions of warfare. An excellent example of this is a paper by T Ganelius (202), in which movement of the front during battle is analyzed using partial differential equations. In the 50's several other scientists at FOA, e.g. B Jansson (297) and L Zackrisson (617, 618, 620) were

well acquainted with Lanchester theory and its ramifications. The first researchers in Sweden to deal with Lanchester theory, however, would seem to be H Wallman et. al. (576).

In the 1950's and 60's larger models were created for evaluation of different weapons systems during the test and evaluation phases. In the early '60's the tendency was to use computer simulations and - for assessment of ground battles - ordinary gaming, where different "score methods" were used instead of Lanchester equations. Simulations of ground battle using computers were at a low organizational level, using hit probabilities and geometrical descriptions for the movement of soldiers, tanks etc. In the beginning of the 1970's, operations research teams within the military services (manned by FOA) became involved in problems at a high organizational level (the total military defense structure or a whole service) and interest in Lanchester theory waned.

At the end of the 1970's interest reappeared, however, when insight was gained in the hierarchy of models developed at the Defence Operational Analysis Establishment (DOAE) in the United Kingdom. Of special interest was a method used by D P Dare and D A P James (137) to aggregate measures of effectiveness from a low organizational level to higher levels. The problem of aggregation has gained new emphasis among defense analysts and been fiercely discussed during the 80's as well as the 90's.

Although several researchers at FOA (G Borenius (77, 78), S Wrigge (610-615) and others) have maintained - and to some extent increased - FOA's knowledge of Lanchester theory and similar subjects, it must be acknowledged that the advanced level of the 1950's and 60's has not been sustained. The amount of work required in order to understand and make use of new developments in Lanchester theory has been underestimated. A contributing factor may be disappointments after earlier efforts to use the theory yielded less than had been expected.

# 2.3 Eastern Europe and the former Soviet Union

Owing to the language barrier and a strong inclination for secrecy, it has been difficult to gain a clear view of the situation on the "Lanchester front" in the countries constituting the former Warsaw Pact. It is, however, safe to say that these countries have closely followed what has been published internationally

on Lanchester theory. Soviet textbooks on operations research mention Lanchester equations - deterministic as well as stochastic - as standard methods to predict the outcome of battle. Researchers who have studied the subject in detail, e.g. J W Stirling and J W Anderson<sup>1</sup>, are of the opinion that Soviet practitioners of operations research often use theories published in the West, nor have they found there any ideas or theories unknown to Western countries.

Our knowledge of the use of Lanchester theory in the East has increased somewhat since 1975. One should mention contributions by Yu V Chuyev (116), F I Eresko (169), V.M. Gavrilov (208), R L Helmbold (264), V F Krapivin (345), M Osipov (408), P N Tkachenko (569), and V N Zhukov (623). It is from Chuyev that we first learn of Osipov as one of the pioneers of the mathematical theory of combat. R L Helmbold (264) has written about Osipov's life (what little is known) and his pioneering work from 1915. Osipov's work is an example of sound military science, and had his theoretical development been available earlier in the West, a great deal of our analyses of attrition warfare would have been unnecessary. As the saying goes, Osipov was remarkably ahead of his time.

We end this section with a quotation from PHALANX, March 1992, about Osipov:

"One way to appreciate Osipov is to contrast his work with that of F W Lanchester, who has long been credited with inventing the square and linear law equations that bear his name. His approach is expository and didactic; in other words, he makes no effort to substantiate mathematical logic with data. Osipov in good old fashioned Russian military scientific fashion, derives his equations as theory, then sets about to test the theory with data from 38 battles, then draws conclusions for the pragmatic purpose of aiding those in command of forces of combat."

<sup>&</sup>lt;sup>1</sup> J W Stirling and J W Anderson, Operations Research in the Warsaw Pact armed forces, Proc 12th US Army Operations Research Symposium, pp 41-48.

#### 3. Sources of information

The references in this bibliography can be presented in three ways, depending on whether one wishes to concentrate on authors, publications or institutions. What follows is a combination of three aspects.

Starting with deterministic Lanchester theory, the most prolific author has been J G Taylor (501-562), who for many years worked at the Naval Postgraduate School in California, USA, which has published most of his research reports. Most of his papers have been published in Naval Research Logistics Quarterly and Journal of the Operations Research Society of America (JORSA). The latter is the journal containing the greatest number of articles on the subject. The frequency of articles on Lanchester theory has, however, declined during the past ten years.

It may be worth mentioning here that the number of publications by J G Taylor and the number of M S theses from the Naval Postgraduate School add up to more than 100, i.e. about a sixth of all references in this report.

On the subject of stochastic Lanchester equations, A F Karr (311-328) is a well-known name. He has been employed at the Institute for Defense Analyses in Virginia, USA. Interesting results have been published by N Jennings (299, 300) and T G Weale (580-587) at DOAE in the United Kingdom. Important work has also been done by C J Ancker and A V Gafarian (19), which includes an annotated bibliography on stochastic Lanchester equations.

A prolific author on the subject of stochastic duels is C J Ancker (8-20), who has worked at the Systems Development Corporation in California, US. Papers by his co-author A V Gafarian (see above), should also be mentioned (198-200).

Another productive scientist is R L Helmbold (248-266), who has worked at several institutes, among them RAND Corporation in California and US Army Concepts Analysis Agency in Maryland, USA. He has, among other things, compared historical data with predictions using Lanchester theory. The RAND Corporation was at an early stage interested in the mathematical theory of combat - see e.g. O Helmer (267), T E Oberbeck (401, 402), and R N Snow

(484). After an interval of low interest, this institute has returned to the subject, although now focusing on problems at a more abstract level - see e.g. P K Davis and D Blumenthal (141).

Leaving aside the pioneering work of M Osipov from 1915, the first effort to validate Lanchester models seems to have been made by J H Engel (162) in 1954, then at the Massachusetts Institute of Technology in USA. Interesting models of battles of the US Civil War have been developed by H K Weiss (594). A mathematical analysis of 60 battles during the Second World War was made by J B Fain (173). Important results also come from D S Hartley at the Oak Ridge National Laboratory in Tennessee (237-244).

Contributions to the area of validation by D Willard (597), J W R Lepingwell (362) and R L Helmbold (see above) should also be mentioned. Generally, it is fair to say that Lanchester theory is underdeveloped in this respect and that this has contributed to its stagnation.

In Western Europe most military research institutes have at times dealt with Lanchester theory. At FOA e.g., approximately 30 reports related to Lanchester theory have been published. We have already mentioned DOAE in the United Kingdom and SACLANT ASW Research Centre in Italy. An overview of what has been published at different institutes is given in *Appendix B*.

One way to follow what is published about Lanchester theory is to read the following publications: JORSA, Naval Research Logistics Quarterly, Government Reports Announcements (GRA) - especially area 15 - and Operations Research: Literatuuroverzicht Wetenschappelijk. The last two publications mentioned give references to reports from NATO countries. Some articles of interest may also be found in the Journal of Canadian Operations Research and the Operational Research Quarterly.

During the last ten years we have also been using computers to search for references in various databases. The results of such searches depend, of course, on how search questions are framed and on which databases are used. Our experience is that all computer searches must be supplemented by manual investigations and literature studies. Also, through the years, many valuable

Lars Wigg Staffan Wrigge

references have been given to us by colleagues at FOA and elsewhere. We want to take the opportunity here to thank all of them.

Although we have been collecting references to Lanchester theory for some twenty years - and publish here the results of our common efforts - we can hardly claim that this bibliography is in any way complete. It is our hope, however, that we have included the most valuable publications on Lanchester theory and related subjects, and that our readers will benefit from this overview.

# 4. Use of the bibliography

The main body of the bibliography (Appendix A) is a numbered listing of references to books, theses, reports, articles etc, where the authors are listed in alphabetical order. To facilitate use of the bibliography, the reference numbers have also been grouped under various headings. This material is found in Appendix B. References to e.g. duels, stochastic Lanchester models, RAND Corporation reports, reports from the Naval Postgraduate School can be found here.

# APPENDIX A

#### 0. Preface

In this appendix we give the entire listing of references to papers treating Lanchester and related subjects.

In order to facilitate for the reader we have tried to give enough information in each quoted reference. Thereby we have used some abbreviations, which are listed in Section 1 below.

Section 2 shows the abbreviations used for journals and magazines used as well as country of origin. Section 3 is a listing of the agencies, institutes, universitites etc which have published the reports. Also for the benefit of the reader we have supplied a list of conferences in Section 4 as well as a list of publishers of books in Section 5. A list of acronyms for report identification will be found in Section 6.

The complete listing of references is given in lexicographic order with respect to the authors' surnames in Section 7. To indicate the accuracy of the information the reference number is written in bold type when we actually have seen the document in question. At the end of this section is a complement showing references which were found after the main list had been compiled.

Section 8 gives information about literature, which is referred to in some of the references in section 7.

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# 1. List of abbreviations used

Amer	American
Appl	Applied
Assoc	Association
Bull	Bulletin
Canad	Canadian
Co.	Company
Conf	Conference
Contrib	Contribution
Corp	Corporation
ed	Editor
eds	Editors
esp	Especially
Inc.	Incorporated
Inst	Institute
Int	International
J	Journal
Lab	Laboratory
Labs	Laboratories
Log	Logistics
Ltd.	Limited
M S	Master of Science
Mat	Matematyki
Mathl	Mathematical
Maths	<b>Mathematics</b>
Memo	Memorandum
Mil	Military
No	Number
Opnl	Operational
Opns	Operations

OR Operations Research Doctor of Philosophy Ph D Postgraduate Postgr **Pages** pp Probability Prob Proceedings Proc Quarterly Quart Rep Report Research Res Rev Review Roy Royal Sci Science Scis Sciences Ser Series Soc Society Statl Statistical Stats **Statistics** Symposium Symp Technl Technical Techno Technology **Transactions Trans** US United States Univ University Vol Volume versus vs Zastos Zastosowania

## 2. List of journals and magazines:

Advances in Game Theory

Advances in Game Theory (U S A)

Allgemeinen Schweizerischen Militärzeitschrift (ASMZ)

Allgemeinen Schweizerischen Militärzeitschrift (ASMZ)

Huber & Company Aktiengesellschaft, Presseverlag,

8500 Frauenfeld (Switzerland)

Amer Scientist

American Scientist (USA)

**Annals Mathl Studies** 

Annals of Mathematical Studies (U S A)

Annals of Opns Res

Annals of Operations Research (U S A)

Appl Stats

Journal of the Royal Statistical Society, Series C,

Applied Statistics (U K)

Army

Army (USA)

Artilleri Tidskrift

Artilleri Tidskrift (Sweden)

Behavioral Sci

Behavioral Science (USA)

Bull Amer Mathl Soc

Bulletin of the American Mathematical Society (USA)

**Bull IMA** 

Bulletin of the Institute for Mathematical Analysis (U K)

**Bull Mathl Statistics** 

Bulletin of Mathematical Statistics (U S A)

Bull de la Societe Royale Belge des Electriciens

Bulletin de la Societe Royale Belge des Electriciens (Belgium)

Cahiers du Centre d'Etudes de Recherche Opérationnelle, Bruxelles

Cahiers du Centre d'Etudes de Recherche Opérationnelle,

c/o Institut de Statistique de l' U. L. B.,

C. P. 210 - Boulevard du Triomphe,

1050 Bruxelles - Belgique (Belgium)

Colloquium Mathematicum

Colloquium Mathematicum (Poland)

Computational and Opns Res

Computational and Operations Research (U K)

Cybernetics - in the Service of Communism

Cybernetics - in the Service of Communism (?)

Defence Sci J

Defence Science Journal (India)

Defense Analysis

Defense Analysis (U K)

DTIC

DTIC (?)

Elementa

Elementa (Sweden)

European J Opnl Res

European Journal of Operational Research (The Netherlands)

History, Numbers and War

History, Numbers and War (U S A)

Int J Systems Sci

International Journal on Systems Science (U S A)

Int Security

International Security (U S A)

Jahrbuch der Wehrtechnik

Jahrbuch der Wehrtechnik (Germany)

J Amer Statl Assoc (JASA)

Journal of the American Statistical Association (U S A)

J Appl Prob

Journal of Applied Probability (U K)

J Canad Opnl Res Soc (CORS)

Journal of the Canadian Operational Research Society (CORS)

(Canada)

J Conflict Resolution

The Journal of Conflict Resolution (U S A)

J Franklin Inst

Journal of The Franklin Institute (U S A)

J Mathl Analysis and Applications (JMAA)

Journal of Mathematical Analysis and Applications (U S A)

J Opnl Res Soc

Journal of the Operational Research Society (U K)

J Opns Res Soc Japan

Journal of the Operations Research Society of Japan (Japan)

J Roy Aeronautical Soc

Journal of the Royal Aeronautical Society (U K)

J Roy Statl Soc A

Journal of the Royal Statistical Society, Series A (U K)

J Roy United Services Inst for Defence Studies Quart (RUSI)

Journal of the Royal United Services Institute for Defence

Studies Quarterly (RUSI) (U K)

Management Sci

Management Science (USA)

Der Matematikunterricht

Der Matematikunterricht (?)

Mathl and Computer Modeling

Mathematical and Computer Modeling (U S A)

Mathl Modeling

Mathematical Modeling (U S A)

Mathl Scientist

The Mathematical Scientist (Australia)

Memoirs Defense Academy Japan

Memoirs of the Defense Academy of Japan (Japan)

**MIC** 

MIC (?)

Mil Rev

Military Review (USA)

Nature

Nature (U K)

Naval Res Log

Naval Research Logistics (USA)

Naval Res Log Quart

Naval Research Logistics Quarterly (U S A)

Normat

Normat (Scandinavia)

Numerical Methods in Partial Differential Equations

Numerical Methods in Partial Differential Equations

Obituary Notices of the Fellows of Roy Soc

Obituary Notices of the Fellows of Royal Society (U K)

Opnl Res Quart

Operational Research Quarterly (U K)

Opns Res

(Journal of) Operations Research (U S A)

Opns Res Spektrum

Operations Research Spektrum (U S A)

Opsearch

Opsearch (U S A)

Organizational Behaviour in Human Performance

Organizational Behaviour in Human Performance

OR Overzicht TDCK

Operations Research Literatuuroverzicht TDCK.

's-Gravenhage (The Netherlands)

**PHALANX** 

PHALANX (The Bulletin of Military Operations Research

Society), Alexandria, Virginia (U S A)

Proc U S Naval Inst

Proceedings of the United States Naval Institute (U S A)

Quality Control and Appl Statistics

Quality Control and Applied Statistics (U S A)

Sankhya B

Sankhya, Series B (India)

SIAM J Appl Maths

Society of Industrial and Applied Mathematics Journal on Applied Mathematics (U S A)

SIAM Rev

Society of Industrial and Applied Mathematics Review (U S A)

Signal

Signal (Journal of the Armed Forces Communications and

Electronics Association) (USA)

Synthese

Synthese (?)

Teknisk Tidskrift

Teknisk Tidskrift (Sweden)

Trans of the New York Academy Of Sciences

Transactions of the New York Academy of Science, Series II (U S A)

War Gaming Cosmagon and Zigspiel

War Gaming Cosmagon and Zigspiel (?)

Zastos Mat

Zastosowania Matematyki (Poland)

Zeitschrift für Angewandte Mathematik und Mechanik (ZAMM)

Zeitschrift für Angewandte Mathematik und Mechanik (ZAMM)

(West Germany)

Zeitschrift für Opns Res

Zeitschrift für Operations Research (Germany)

#### 3. List of institutes

Admiralty Underwater Weapons Establishment

Amer Mathl Soc

Army Command and General Staff College

Army Material Systems Analysis Activity

Ballistic Res Labs

The BDM Corp

The Brookings Institution

Brooks Air Force Base

- School of Aerospace Medicine

Brunel Univ

Carnegie-Mellon Univ

- Department of Statistics

Center for Naval Analyses

Colorado Univ

- Department of Maths

Combined Arms Opns Res Activity

Convair

Defence Materiel Administration (FMV)

Defence Operational Analysis Establishment

Department of the Air Force

Department of National Defense, Canada

Douglas Aircraft Company, Inc.

"Energija"

Florida State Univ

- Department of Statistics

George Washington Univ

Georgia Inst Techno

Government Printing Office

Inst for Defense Analyses

- Program Analysis Division

Institut für strategische Grundlagenforschung an der

Landesverteidigungsakademie des Bundesministeriums für

Landesverteidigung

Iowa Univ

- Department of Statistics

Johns Hopkins Univ

- Department of Mathl Sciences
- Opns Res Office

Joint Publications Res Service

Lambda Corp

Lawrence Livermore National Lab

Louisiana Technical Univ

- College of Administration Business
  - Department of Business Analysis Communication

Martin Marietta Energy Systems, Inc.

- Oak Ridge Gaseous Diffusion Plant

#### Massachusetts Inst Techno

- Lab for Information and Decision Systems
- Opns Res Group

Messerschmitt-Boelkow-Blohm G m b H

- Unternahmensbereich Apparate

Ministry of Defence

- Center for Mil Analyses

National Bureau of Standards

National Defence Res Establishment (FOA)

National Res Council

- Committee on Amphibious Opns

Naval Ordnance Lab

**Naval Postgr School** 

Naval War College

- Center for Advanced Res
- Department of Opns

Naval Weapons Center

North Amer Aviation

Northeastern Univ

- Electronics Res Lab

Oak Ridge K-25 Site

Oak Ridge National Lab

Office of Scientific Res and Development

Ohio State Univ

- Department of Industrial Engineering
- Systems Res Group

Opns Res Gruppe der IABG

The Pentagon

- Organization of the Joint Chiefs of Staff

Physics and Electronics Lab

**RAND Corp** 

Res Analysis Corp

Roy Inst Techno

- Department of Automatic Control

Roy Mil College Sci

SACLANT ASW Res Centre

Sandia Labs

SHAPE Technical Centre

**Synectics Corp** 

System Development Corp

Tactical Weapon Guidance and Control Information and Analysis

Center

Technical Opns, Inc.

- Combat Opns Res Group

Univ California

- Department of Economics

Univ Hull

- Department of Mathl Statistics and Subdepartment of Opns Res

Univ Maryland

- Physics Department

Univ Michigan

- Systems Res Lab

. Department of Industrial Engineering

Univ Microfilms

Univ Microfilms Int

Univ Southern California

- Department of Electrical Engineering

Univ South Florida

U S Air Force Systems Command

U S Army Concepts Analysis Agency

U S Army Engineer School Readings Opns Res/Systems Analysis

U S Army TRADOC Analysis Command

U S Army Weapons Command

- Systems Analysis Directorate Corp

U S Government

Virginia Polytechnic Inst

Wright-Patterson Air Force Base

- Foreign Techno Division

- U S Air Force Inst Techno

. School of Engineering

. School of Systems and Logistics

Zentrale Operations-Research-Stelle

#### 4. List of Conferences

- 1. Advances in Game Theory, Annals of Mathematical Studies 52 1964
- 2. Annual Meeting of the Operations Research Society in U S A 23th 40th
- 3. Annual United States Army Operations Research Symposium 4th 10th 11th 12th 13th 17th
- 4. Conference of Army Mathematics 24th
- 5. Carl-Cranz-Gesellschaft Meeting on Bewertung von Waffensystemen November 29, 1974
- 6. Fire Support Method Methodology Workshop 1975
- 7. IFORS International Conference on Operations Research 8th
- 8. International Conference on Operational Research 1st 2nd 4th 5th 11th
- International Symposium on Applied Computations of Operations Research to Problems of World Concern 1973
- Los Angeles Joint National Meeting November 13-15, 1978
- 11. Meeting of SIAM November 2-4, 1961
- 12. Military Operations Research Symposium 8th 14th 35th 57th
- 13. MIT/ONR Workshop on C3 Systems
- National Meeting, Military Applications Section, Operations Research Society of America
   1st
- 15. NATO Conference on Modeling Land Battle Systems in Military Planning August 1974
- 16. NATO Conference on Recent Developments in Lanchester Theory July 3-7, 1967
- 17. Operations Research Society Annual Conference September 6-7, 1979
- 18. Symposia in Applied Mathematics Volume 25
- 19. University of Michigan Engineering Summer Conference on Military Operations Research
- July 21-August 1, 1969
  20. United States Army Engineer School Readings in Operations Research/Systems
  Analysis
  January 1969
- 21. Winter Simulation Conference December 4-6, 1989

#### 5. List of Publishers

- 1. American Mathematical Society, Providence, Rhode Island
- 2. Constable and Co, London
- 3. Elsevier Publishing Co, New York
- 4. Gordon & Breach Science Publishers, New York
- 5. Hero Books, Fairfax, Virginia
- 6. John Wiley & Sons, New York
- 7. MacDonald and Jane's Publishers Ltd, London
- 8. National Bureau of Standards, Gaithersburg, Maryland
- 9. North-Holland, Amsterdam, The Netherlands
- 10. Paragon Publishers, New York
- 11. Plenum Press, New York
- 12. Quadrangle Books, Chicago
- 13. R Oldenbourg Verlag, München, West Germany
- 14. Springer Verlag, Berlin, Germany
- 15. The Boxwood Press, Pittsburgh
- 16. The Principia Press, Inc, Bloomington, Indiana
- 17. UNIBOOKS English Universities Press, London

#### 6. List of report identifications

AF US Air Force

AFIT Air Force Institute of Technology

AFOSR (Iowa University)
ARO Army Research Office
BD The BDM Corporation

BRL Ballistic Research Laboratories

CAA U S Army Concepts Analysis Agency

CEMA Center for Military Analyses
CNA Center for Naval Analyses

CORG Combat Operations Research Group

DAAB U S Army STAG

DOAE Defence Operational Analysis Establishment, United Kingdom FDOK Flygdokumentation, Defence Material Administration, Sweden

FEL Physics and Electronics Laboratory

FOA National Defence Research Establishment, Sweden

GACIAC Tactical Weapon Guidance and Control Information and Analysis Center

IDA Institute for Defense Analyses

ISE ???

K Oak Ridge K-25 Site

LIDS Laboratory for Information and Decision Systems
MBB Messerschmitt-Boelkow-Blohm GmbH, Germany

MCOAB Center for Naval Analyses
NBS National Bureau of Standards
NPS Naval Postgraduate School
NWC Naval Weapons Center

ORG Operations Research Gruppe der IABG, Germany

ORNL Oak Ridge National Laboratory
ORO Operations Research Office

R RAND Corporation

RF ???

SACLANTCEN SACLANT ASW Research Centre
SP System Development Corporation
SRL Systems Research Laboratory
STC SHAPE Technical Centre
TPA North American Aviation

TRASANA Army TRADOC Analysis Command
TRITA The Royal Institute of Technology, Sweden

UC University of California

USAF US Air Force

WSEG Weapons Systems Evaluation Group

ZOR Zentrale Operations-Research-Stelle, Germany

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Before finishing this bibliography an extra effort was made to cover the subject more completely. This has resulted in the following complement. This is organized in the same way as the main bibliography but has received its own numbering sequence. The reference numbers are preceded with the letter "C" (short for Complement). Many of the additional references are descriptions of computer models of battles from battalion to theater level.

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## APPENDIX B

In this Appendix ordinary numbers and numbers preceded by the letter "C" refer to section 7 of Appendix A. Numbers preceded by an "R" refer to section 8.

## 1. References classified according to subject matter

# a. Allocation of fire etc

(21), (28), (159), (224), (330), (346), (387), (445), (458), (495), (497), (501), (506), (512), (514), (625), (C4), (C43), (C61)

## b. Analyses of historical data, validation etc.

(6), (19), (29), (49), (50), (79), (99), (112), (119), (155), (156), (162), (164), (173), (174), (176), (180), (217), (237), (238), (240), (241), (242), (244), (248), (249), (250), (251), (252), (254), (256), (260), (261), (262), (263), (266), (293), (339), (340), (362), (375), (376), (397), (409), (410), (420), (424), (426), (441), (449), (460), (461), (465), (492), (592), (594), (597), (C10), (C18), (C19), (C22), (C48), (C54), (C57), (C70), (C71)

## c. Biographical data

(264), (308), (338), (350), (351), (373), (408), (440)

## d. Command, control, communication and information

(175), (207), (372), (388), (468), (498), (511), (571), (606), (608), (R27)

## e. Comparison of deterministic and stochastic models

(83), (91), (234), (320), (342), (360), (394), (422), (423), (562), (595)

### f. Deterministic Lanchester models

(1), (33), (34), (37), (39), (40), (43), (46), (61), (62), (63), (64), (65), (66), (82), (86), (87), (89), (90), (91), (97), (102), (103), (106), (114), (122), (126), (132), (135), (136), (138), (144), (149), (162), (163), (168), (169), (171), (172), (181), (194), (195), (202), (217), (218), (225), (226), (227), (230), (233), (245), (253), (255), (265), (276), (285), (302), (306), (307), (309), (310), (320), (329), (345), (348), (350), (351), (352), (356), (357), (358), (361), (363), (364), (365), (367), (369), (371), (372), (374), (377), (379), (386), (389), (391), (392), (399), (401), (402), (411), (412), (418), (419), (425), (427), (428), (429), (432), (436), (445), (456), (459), (463), (464), (475), (483), (484), (485), (486), (487), (489), (502), (503), (504), (507), (509), (513), (515), (518), (520), (523), (525),

(526), (527), (531), (532), (533), (536), (537), (541), (542), (543), (545), (546), (547), (548), (550), (551), (552), (553), (554), (555), (556), (557), (558), (559), (560), (561), (563), (575), (576), (588), (589), (598), (608), (610), (611), (612), (613), (619), (620), (R24)

#### g. Duels

(8), (9), (10), (11), (12), (13), (14), (15), (16), (17), (18), (20), (41), (42), (44), (45), (51), (52), (53), (127), (186), (189), (190), (191), (193), (196), (197), (199), (200), (209), (221), (257), (332), (336), (337), (346), (347), (353), (354), (407), (437), (450), (471), (479), (481), (496), (499), (500), (564), (566), (577), (599), (600), (601), (602), (603), (C33)

### h. Duration of battles and strikes

(18), (83), (278), (349), (390), (395), (396), (457), (583), (593)

## i. Games

(30), (31), (57), (79), (107), (159), (169), (181), (197), (228), (283), (288), (289), (291), (298), (303), (304), (330), (331), (345), (387), (439), (443), (458), (461), (477), (501), (506), (510), (512), (514), (519), (524), (590), (609), (617), (618), (621), (C5), (C6), (C7), (C30), (C60), (C62), (C67), (R5)

### j. Markov chains and similar approaches

(41), (42), (44), (45), (294), (335), (438), (454), (455), (578), (591), (621), (C64)

### k. Models of air combat

(109), (160), (178), (179), (180), (194), (195), (197), (210), (220), (223), (259), (303), (304), (350), (352), (357), (359), (403), (410), (437), (482), (566), (C1), (C2), (C3), (C4), (C6), (C10), (C13), (C15), (C16), (C25), (C26), (C35), (C36), (C38), (C40), (C42), (C43), (C46), (C55), (C73)

### 1. Models of guerilla and small units combat

(1), (5), (121), (134), (144), (182), (284), (307), (412), (464), (478), (483), (487), (489), (490), (C53)

#### m. Models of naval operations

(87), (98), (101), (129), (136), (183), (184), (220), (231), (232), (290), (293), (347), (381), (596), (625), (C47), (C62)

#### n. Overviews, surveys and bibliographies

(10), (13), (16), (19), (40), (65), (68), (69), (100), (116), (149), (151), (158), (177), (187), (213), (226), (229), (246), (262), (301), (302), (393), (473), (474), (475), (485), (516),

(528), (529), (538), (539), (540), (544), (574), (614), (615), (C22), (C41), (C57), (C63), (R24)

## o. Stochastic models and simulation

(7), (8), (9), (10), (11), (12), (13), (14), (15), (16), (17), (18), (20), (32), (36), (41), (42), (51), (52), (53), (55), (56), (77), (78), (79), (80), (81), (93), (94), (95), (96), (111), (113), (121), (123), (124), (130), (138), (139), (142), (145), (153), (181), (186), (198), (199), (200), (214), (215), (216), (220), (222), (258), (276), (277), (286), (294), (295), (299), (300), (305), (307), (313), (314), (315), (316), (317), (319), (320), (321), (331), (335), (341), (344), (348), (366), (368), (381), (407), (414), (415), (416), (438), (446), (447), (450), (451), (452), (453), (454), (455), (466), (467), (469), (472), (476), (477), (480), (486), (487), (488), (489), (566), (570), (578), (579), (580), (581), (582), (583), (584), (585), (586), (587), (591), (593)

## o. Strikes, struggle for market shares

(110), (115), (278), (349), (378), (390), (385), (396), (457)

## 2. References classified according to publishing institution

Institutions with fewer than four publications have not been included here. Underlined numbers refer to M S theses.

### a. Aberdeen Proving Ground

(124), (125), (126), (221), (588), (C27)

#### b. Air Force Institute of Technology (AFIT)

(112), (355), (357), (430), (472)

#### c. Carnegie-Mellon University

(142), (414), (415), (416)

## d. Center for Naval Analyses (CNA)

(87), (164), (176), (180), (231), (232), (364), (403), (409), (410)

## e. Concepts Analysis Agency (CAA)

(262), (263), (266), (408), (616), (C14)

## f. Defence Operational Analysis Establishment (DOAE)

(83), (137), (145), (215), (230), (299), (300), (580), (581), (582), (583), (584), (587), (C76). Cf also (324).

## g. FOA (National Defence Research Establishment)

(77), (78), (80), (167), (181), (193), (219), (223), (227), (290), (298), (389), (398), (610), (611), (612), (613), (614), (615), (619), (620)

## h. Institute for Defense Analyses (IDA)

(21), (22), (23), (24), (25), (26), (27), (28), (54), (171), (311), (312), (313), (314), (315), (316), (317), (318), (319), (321), (322), (323), (324), (325), (326), (327), (328), (C1), (C2), (C35), (C36), (C70), (C71), (C72)

## i. Johns Hopkins University

(49), (50), (57), (95), (105), (119), (122), (201), (236), (320), (358)

## j. Naval Postgraduate School

(2), (29), (46), (47), (55), (56), (91), (98), (102), (103), (104), (106), (111), (114), (131), (132), (133), (134), (146), (159), (177), (182), (192), (207), (224), (229), (234), (235), (273), (282), (284), (333), (342), (359), (360), (361), (363), (369), (374), (379), (380), (388), (394), (399), (404), (412), (413), (417), (422), (436), (438), (443), (443), (459), (474), (479), (482), (483), (494), (497), (498), (501), (503), (506), (507), (511), (512), (514), (517), (519), (520), (521), (526), (527), (528), (529), (531), (533), (535), (536), (537), (538), (539), (544), (548), (549), (550), (552), (553), (554), (555), (556), (558), (559), (562), (571), (578), (595), (609), (622), (C12), (C31), (C32), (C39), (C43), (C53), (C55), (C62), (C63), (C66), (R28)

## k. Oak Ridge National Laboratory (ORNL)

(33), (34), (35), (135), (237), (285), (424), (425), (426), (427), (429), (456), (462), (470)

### 1. Ohio State University

(61), (120), (121), (C9), (C11), (C54)

### m. RAND Corporation

(141), (160), (210), (258), (259), (260), (267), (269), (270), (289), (401), (402), (431), (448), (463), (471), (484), (C7), (C15), (C26), (C48), (C57)

#### n. Research Analysis Corporation (RAC)

(331), (597), (C8), (C17), (C37), (C38)

### o. SACLANT ASW Research Centre

(92), (129), (172), (245), (347), (381), (386), (596), (C47)

## p. SHAPE Technical Centre

(113), (405), (406), (607), (C23)

# q. System Development Corporation

(8), (11), (599), (600), (601)

# r. Technical Operations, Inc.

(143), (248), (250), (251)

# s. University of Michigan

(63), (64), (74), (75), (94), (495), (R2), (R3)

# t. Vector Research, Inc.

(C25), (C46), (C68), (C69)